Metal Ion-Aromatic Complexes. IV. Five-Coordinate Silver(I) in $C_6H_6 \cdot AgAlCl_4$

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Abstract: A new silver(I)-benzene complex ($C_6H_6 \cdot AgAlCl_4$) has been prepared and its crystal structure determined by three-dimensional photographic single-crystal X-ray diffraction techniques. In contrast to the pleated sheet structure of C₆H₆·CuAlCl₄, the structure of C₆H₆·AgAlCl₄ is made up of infinite planar sheets composed of AlCl₄tetrahedra connected by Ag-Cl bonds with π -type Ag(I)-aromatic interactions perpendicular to the sheet. This arrangement gives Ag(I) a coordination number of five: four Ag-Cl interactions at 2.59, 2.77, 2.80, and 3.04 A, all ± 0.02 A, and one Ag-C₆H₆ interaction with Ag to the center of the nearest C-C bond, a distance of 2.57 \pm 0.06 A. Each Ag(I) species is bonded to only one benzene ring such that the dihedral angle between the benzene ring plane and the plane defined by silver with its two nearest carbon neighbors is 98°. However, these shorter Ag-C distances are unequal at 2.92 and 2.47 A, both ± 0.06 A. All other interatomic distances correspond to normal van der Waals distances.

The existence of a number of silver(I)-aromatic complexes of varying degrees of stability was demonstrated some time ago by the solubility measurements of Andrews and Keefer.³ The gross geometrical features of the silver(I)-benzene interaction in the silver perchlorate-benzene complex were predicted by both Mulliken⁴ and Dewar⁵ and verified by the structure investigation of Smith and Rundle.6 However, this structure has several unusual features; e.g., either a large anisotropic thermal motion or a statistical disordering of the Ag atoms is required, and the benzene ring shows an unusual distortion. In order to better understand the nature of the binding forces in silver-(I)-aromatic complexes as well as to clarify the reported unusual features of the silver perchlorate-benzene complex, we have prepared a number of hitherto unknown crystalline complexes of the type ArAgX, where Ar represents a variable aromatic donor and X a variable anion. This is part of a general program of investigation of the structure of metal ion-aromatic complexes in which the effect of the following factors on complex formation is being investigated: (1) the electronic structure and energy levels of the metal ion and the aromatic system; (2) metal ion-anion interactions; (3) steric factors; and (4) molecular packing, at least in the solid state. As part of this research, we have prepared C6H6·AgAlCl4 and have found no simple relationship in terms of space group or cell dimensions between this compound and C₆H₆·CuAlCl₄^{7,8} or C₆H₆·AgClO₄.⁶ We undertook a single-crystal X-ray structure analysis to determine the stereochemistry of the C₆H₆·AgAlCl₄ complex and also to further our understanding of the nature of the bonding between the metal ion and the aromatic system. The metal-

anion distances would also give more insight into the role of the anion in these complexes.

Experimental Section

C₆H₆·AgAlCl₄ was prepared by treating a slight excess of pure, dried AgCl with 0.03 mole of resublimed AlCl₃ and 20 ml of dried benzene. The procedure for the preparation of this compound and growing of single crystals is very similar to that of C₆H₆·CuAlCl₄; for details see ref 8. There were two complications that arose with $C_6H_6 \cdot AgAlCl_4$ that were not present with $C_6H_6 \cdot CuAlCl_4$: (1) the crystals had to be grown in the dark to avoid photochemical decomposition of the silver ion; and (2) it was very difficult to obtain suitable single crystals for diffraction studies. The crystals had a marked tendency to twin, and over a period of 3 years more than 100 crystals were examined until one was found to be sufficiently free of twinning to justify a single-crystal structure analysis. As with C₆H₆·CuAlCl₄, the chemical analyses were only sufficiently accurate to indicate the correct stoichiometry.

A crystal of approximately $0.35 \times 0.30 \times 0.40$ mm was used to collect 496 independent hkl observed intensities by standard multiple film equiinclination Weissenberg techniques from hk0, hk1, . hk5 levels with Zr-filtered Mo K α radiation. In addition, h0land 0kl precession-timed exposure intensity data were collected with Zr-filtered Mo K α radiation and used for preliminary scaling of the three-dimensional Patterson and electron density calculations. Intensities were measured with a calibrated strip. The linear absorption coefficient (μ) for C₆H₆·AgAlCl₄ with Mo Kα radiation is 28 cm⁻¹. Since some surface decomposition was unavoidable and the absorption due to this decomposition could not be readily calculated, no corrections for absorption were made.

Calculations were made with an IBM 7090. Patterson and Fourier calculations were made with the Sly-Shoemaker-Van den Hende program. The refinement was carried out by full-matrix least squares with the Hughes 10 weighting scheme with $4F_{\min} = 15$. We minimized the function $\Sigma w(F_{\circ} - F_{\circ})^2$. Atomic scattering factors were taken from the compilation of Ibers¹¹ for Ag⁺, Cl⁻, Al3+, and neutral C.

Results

Unit Cell and Space Group. C₆H₆·AgAlCl₄ was found to crystallize in the monoclinic crystal system. With Mo K α (0.7107 A), cell constants were obtained from precession photographs: a = 9.09, b = 10.22, $c = 12.73 \text{ A (all } \pm 0.03 \text{ A)}, \text{ and } \beta = 95^{\circ} 05' \pm 15'.$ The observed systematic extinctions (for h0l, l = 2n+ 1; and for 0k0, k = 2n + 1) uniquely specify the space group as P21/c. With four C6H6·AgAlCl4

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entities per cell, the calculated crystal density was found to be 2.01 g cm⁻³. No density determination was made, but the cell volume of 1176 A^3 is very close to the 1123 A^3 found for $C_6H_6 \cdot CuAlCl_4$, which has been shown to have four molecules per cell.

Determination of the Structure. The observed intensities were corrected for Lorentz and polarization factors and reduced to squared structure factors for input to the three-dimensional Patterson function.

From the three-dimensional Patterson function it was found that the Ag, four Cl, and Al atoms were in the general positions of $P2_1/c$, $\pm(x, y, z: x, \frac{1}{2} - y, \frac{1}{2} + z)$. The carbon atoms were located from three-dimensional electron density sections with phases based upon the Ag, four Cl, and Al atom coordinates. The structure was refined by least squares until the maximum shift of position coordinates for the last refinement cycle was found to be 0.0003 of the cell edges for the heavier atoms and 0.002 for carbon. The variables were the atomic coordinates, individual isotropic atomic temperature factors, and the scale factors for the isotropic

refinement. For the anisotropic refinement, the Ag and Cl atoms had variable anisotropic temperature factors of the form exp $-(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + 2\beta_{12}hk +$ $2\beta_{23}kl + 2\beta_{13}hl$), but the carbon atoms had only an individual isotropic variable temperature factor. The scale factors were not varied after the isotropic refinement. A final three-dimensional difference map did not indicate any unusual features. The final disagreement index, $R(R = \Sigma ||F_o| - |F_c||/\Sigma |F_o|)$, after refinement was found to be 0.132, and the final weighted disagreement index was 0.168. The standard error of an individual reflection $\{[\Sigma_i w_i (F_c - F_o)^2/(m - n)]^{1/2},$ where m = 496 observations and n = 78 variables upon completion of the refinement was found to be 2.07. Although the value of the disagreement index is somewhat high by modern standards, as are the errors, the stability of the compound and the nature of the crystals are such that we feel that we have done the best analysis possible with the best data we have been able to obtain. Hence, no physical interpretation should be made of the anisotropic temperature factors. The final observed and calculated structure factors are listed in Table I. Final atomic parameters and standard

Table II

Table II													
			P	ositional	and Tempe	rature Pa	rameters and l	Errors ^a					
	Atom	x/c		y/b	_	z/c	$\sigma(x)$		$\sigma(y)/b$		$\sigma(z)/c$		
	Ag		0.1382			0.0323	0.0003		0.0003 0.000		0.0008		
	Cl(1)		0.8527			0.6290	0.0014		0.0015	0.0015 0.0030			
Cl(2)		0.2300		0.4385 0.6		0.6753	0.0014		0.0015		0.0029		
Cl(3)		0.0472		0.6076		0.8651	0.0016		0.0013		0.0031		
(Cl(4)		0.0996		0.7547		0.0018		0.0011		0.0030		
	Al		0.0574		767 0.6998		0.0016 0.0013						
(C(1)		0.5422		0.1120				0.0048				
(C(2)		0.4895		0.1548		0.0052		0.0050	0.0050		0.0101	
	C(3)		0.3532		1289 0.1081		0.0056		0.0056		0.0115		
(C(4)		178	0.3747	0.3747		0.0055		0.0054		0.0107		
	C(5)		0.4458		34 0.9466			0.0054		0.0053		0.0106	
	C(6)		0.5144		0.4805		0.0058 0.00		0.0052	2 0.0102			
				Therma	l Parameter	rs and Sta	andard Deviat	ions					
[Ani	sotropic Ten	nperatur	e Factors of	the Forn	$n \exp -(\beta_1)$	$h^2 + \beta_{22}$	$k^2 + \beta_{33}l^2 + 1$	$2\beta_{12}hk$ -	$+2\beta_{13}hl+2\beta_{13}hl$	$\beta_{23}kl);$	$\sigma' = \sigma \times 10^{\circ}$	4]	
Atom	eta_{11}	σ′	$\boldsymbol{\beta_{22}}$	σ'	eta_{33}	σ'	eta_{12}	σ'	eta_{13}	σ'	$oldsymbol{eta_{23}}$	σ'	
Ag	0.0084	3	0.0081	3	0.0045	7	-0.0004	3	-0.0012	6	-0.0010	7	
Cl(1)	0.0099	16	0.0112	15	0.0058	13	-0.0031	13	-0.0029	27	0.0002	25	
Cl(2)	0.0130	18	0.0099	14	0.0055	15	0.0064	14	-0.0028	28	-0.0030	25	
Cl(3)	0.0129	17	0.0070	13	0.0060	10	0.0021	12	0.0026	30	-0.0013	25	
Cl(4)	0.0211	22	0.0033	13	0.0073	21	-0.0009	12	0.0001	30	0.0004	20	
Al	0.0095	18	0.0033	12	0.0035	17	0.0015	12	0.0027	31	-0.0014	25	
	Carbon a								_				
	temperature factors				Scale								
	Atom		B, A ²			Layer		factor			σ		
C	C(1)		3.47		hk0		0.3253				0.0053		
C	C(2)		5.71			hk1		0.3209			0.0047		
	C(3)		4.18			hk2		0.2745			0.0036		
	C(4)		5.13			hk3		0.1523			0.0048		
	C(5)		5.82		hk4			0.1172			0.0029		
	C(6)		3.68		hk5 0.1)42		0.0060				
F	$(calcd)_{abs} = $	F(C)/(10	\times scale fac	tors)									

^a Numbers in parentheses consistent with subscripts in other tables and figures.

Table III. Distances and Angles for C₆H₆·AgAlCl₄

		Bonded Distances	
Al-Cl ₄	2.13 ± 0.02	Ag-Cl ₄	2.80 ± 0.02
Al-Cl ₃	2.14 ± 0.02	$Ag-Cl_3$	2.77 ± 0.02
$Al-Cl_2$	2.15 ± 0.02	$Ag\text{-}Cl_2$	2.59 ± 0.02
$Al-Cl_1$	2.12 ± 0.02	$Ag-Cl_1$	3.04 ± 0.03
C_1 - C_2	1.31 ± 0.10	$Ag-C_3$	2.92 ± 0.07
C_2 - C_3	1.52 ± 0.08	Ag-C ₄	2.47 ± 0.06
C ₃ -C ₄	1.47 ± 0.16	Ag-midpoint C_3 - C_4	2.57 ± 0.06
C_4 – C_5	1.47 ± 0.12	Nonbonded Intermolecular	
C_5 – C_6	1.21 ± 0.08	Cl ₃ -Cl ₄ 3.97 Cl ₂ -Cl ₃ 4.18	Cl ₁ -C ₄ 3.99
C_6 – C_1	1.42 ± 0.10	Cl_1-Cl_3 4.02 Cl_3-Cl_3 >5.00	Cl ₂ -C ₃ 3.88
	Nonbo	onded Intramolecular Distances, A	<u>-</u> -•
Cl_1-Cl_2	3.50 ± 0.02	Cl_1 – Cl_4	3.39 ± 0.02
Cl_2 – Cl_3	3.50 ± 0.02	$\text{Cl}_3\text{-Cl}_1$	3.51 ± 0.02
Cl ₃ –Cl ₄	3.51 ± 0.02	Cl_2Cl_4	3.49 ± 0.02
	Bor	nded Angles for C ₆ H ₆ ·AgAlCl ₄	
		$\mathrm{Cl_4} ext{-}\mathrm{Ag-}\mathrm{Cl_2}$	$137.2 \pm 0.6^{\circ}$
Cl_1 - Al - Cl_2	$110 \pm 1^{\circ}$	Cl_1 - Ag - Cl_4	$70.3 \pm 0.3^{\circ}$
Cl_1 - Al - Cl_3	$111 \pm 1^{\circ}$	Cl_1 - Ag - Cl_3	$144.0 \pm 0.6^{\circ}$
Cl_2 -Al- Cl_3	$109 \pm 2^{\circ}$	$\mathrm{Cl_2} ext{-}\mathrm{Ag-}\mathrm{Cl_3}$	$103.8 \pm 0.6^{\circ}$
Cl_1 - Al - Cl_4	$106 \pm 2^{\circ}$	Cl_4 - Ag - Cl_3	$79.0 \pm 0.4^{\circ}$
Ag-Cl ₄ -Al	$95.0 \pm 0.6^{\circ}$	$\mathrm{Cl_{1} ext{-}Ag ext{-}Cl_{2}}$	$87.2 \pm 0.5^{\circ}$
Cl_3 - Al - Cl_4	$111 \pm 1^{\circ}$	C_4 – Ag – C_3	$30.0 \pm 4^{\circ}$
$Ag-Cl_1-Al$	$87.7 \pm 0.5^{\circ}$	Cl_1 -Ag-midpoint C_3 - C_4	$118.9 \pm 2^{\circ}$
$Ag-Cl_2-Al$	$93.9 \pm 0.6^{\circ}$	Cl_2 -Ag-midpoint C_3 - C_4	$96.6 \pm 2^{\circ}$
$Ag-Cl_3-Al$	$129.1 \pm 0.6^{\circ}$	Cl_4 -Ag-midpoint C_3 - C_4	$125.9 \pm 2^{\circ}$
C_2 - C_3 -Ag	$98.2 \pm 4^{\circ}$	Cl₃-Ag-midpoint C₃-C₄	$93.8 \pm 2^{\circ}$
C_6 – C_4 – Ag	$95.7 \pm 4^{\circ}$		
	Least-Squares Plane for C ₆	•	
0.7063x +	0.6709y - 0.2259z = 1	$C_1 - 0.090$	$C_4 - 0.080$
		$C_2 + 0.136$	$C_6 + 0.155$
		$C_{3} - 0.065$	$C_6 - 0.071$

deviations are tabulated in Table II. Interatomic distances, angles, 13 and errors are listed in Table III.

Description of the Structure. The crystal structure is composed of sheets of infinite extent in the *bc* plane weakly held together by van der Waals forces. These

⁽¹³⁾ W. R. Busing, K. O. Martin, and H. Levy, OR FFE program.

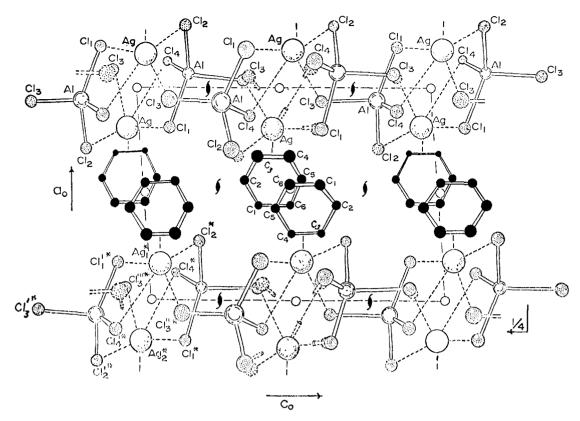


Figure 1. A perspective view down the b(y) axis of the unit cell outlined by dashed lines. Primes denote different $AlCl_4^-$ tetrahedra (b = 1) 10.22 A): Ag₁* at $y \sim b/4$, Ag₂* at $y \sim -b/4$, Cl₂* at $y \sim 0$, Cl₄* at $y \sim -1/4b$, Cl₁* at $y \sim 0$, Cl₄'* at $y \sim 0$, Cl₄'* at $y \sim 0$, Cl₄'* at $y \sim 0$, Cl₃''* at $y \sim b/3$, Cl₃''* at $y \sim b/3$, Cl₃''*

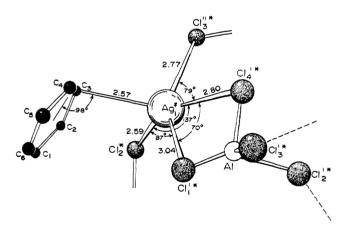


Figure 2. A perspective view of Ag₁* of Figure 1 down the c axis showing the ring coordination geometry and the fivefold coordination of Ag(I). Dotted lines refer to other Ag-Cl interactions.

sheets are composed of AlCl₄⁻ tetrahedra interconnected by silver to chlorine bonds with π -type Ag-C₆H₆ interactions extending out of the sheets (Figure 1). It can be seen from Figure 1 that each Ag(I) species is linked to chlorine atoms of three different tetrahedra in such a manner that each halogen of every AlCl₄entity is involved in a silver-chlorine interaction. For example, Ag_1^* connects $Cl_1'^*$ and $Cl_4'^*$ of one tetrahedron with $Cl_3''^*$ and Cl_2^* of two other $AlCl_4^-$ entities, and Ag_2^* connects Cl_1^* and Cl_4^* of the Cl_2^* tetrahedron with $Cl_2'^*$ and $Cl_3'''^*$ of two tetrahedra. Thus, each silver has four halogen interactions with Cl₂ at 2.59 A, Cl₃ at 2.77 A, Cl₄ at 2.80 A, and Cl₁ at 3.04 A. These interactions, along with the Ag- C_6H_6 π interaction, give Ag(I) the unusual coordination

number of five (Figure 2). All other Ag-Cl interactions are greater than 5 A. However, as the angles indicate, this is a rather irregular fivefold geometry. Inspection of Table III shows that all other distances correspond to only van der Waals interactions. The nearest Ag-C distances are 2.47 and 2.92 A; and the Ag-to-center of nearest C-C bond is 2.57 A, all ± 0.06 A. In contrast to C₆H₆·AgClO₄, each Ag is bonded to only one aromatic ring. Within the relatively large experimental error, the aromatic ring is planar. All the Al-Cl distances are equal within a standard deviation, 2.13 ± 0.02 A.

Discussion

Although there have been several authenticated cases of fivefold coordinated metal ions in the third transition series, 14, 15 these have been generally stabilized by phosphines and/or sterically blocked from further coordination. The most widely known geometries for Ag(I) compounds are: linear, e.g., $Ag(NH_3)_2^+$ and $Ag(CN)_2^{-1}$; tetrahedral, e.g., $Ag[SC(CH_3)NH_2]_4Cl$; 17 or octahedral, e.g., $Ag \cdot 3(O_2C_4H_8) \cdot ClO_4$. However, a number of distorted arrangements of atoms about Ag(I) are also known. 19,20 We know of no previous

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report of a five-coordinate Ag(I) species. From Ag and Cl covalent radii^{21a} a "normal" Ag-Cl single bond would be expected to be 2.51 A. On the other hand, from ionic radii21b one would expect an interatomic separation between Ag(I) and Cl- of 3.06 A. Hence, we feel that the bond distances of 2.59, 2.77, and 2.80 A correspond to varying amounts of covalent character. Although the 3.04-A Ag-Cl₁ distance is long compared to 2.59 A, we feel that this must be considered as something besides a Ag-to-Cl van der Waals interaction for the following reasons: (1) after the Ag-Cl₁ distance of 3.04 A, the next-nearest Ag-Cl distance is greater than 5 A; (2) a more or less tetrahedral environment about the Ag(I) entity would be expected as appears about Cu(I) in C₆H₆·CuAlCl₄;^{7,8} (3) we have observed a similarly long Ag-Cl distance of 3.036 \pm 0.005 A in bis(thiourea)silver(I) chloride22 where there is no doubt that this Cl belongs in the coordination sphere; (4) all the Al-Cl distances are bracketed by 2.13 ± 0.02 A in contrast to the "free" Al-Cl distance of 2.078 ± 0.008 found in $C_6H_6 \cdot CuAlCl_4^{7,8}$ and the 2.07 \pm 0.02 Al-Cl terminal distance in Al₂Cl₆. ²³ However, the 2.13 A compares favorably with the Al-Cl distances of 2.136, 2.141, and 2.153 (all ± 0.007 A) in which the halogen is also bonded to the metal atom in C₆H₈·CuAlCl₄. Although our estimates of bond length errors in both C₆H₆·CuAlCl₄ and C₆H₆·AgAlCl₄ may be somewhat optimistic, and hence the statistical significance of these differences may be marginal, this consistency is striking.

It is clear from the results of this structure analysis that cation-anion interactions must be important in determining the stability of the crystalline complex. Similar results were noted for the cuprous-benzene complex as well. Although using Mulliken's 4 and/or Dewar's 5 theoretical models for the binding in Ag⁺· C₆H₆ complexes gives the correct orientation of the aromatic ring relative to the Ag(I) ion, this must be only fortuitous. Both of these formulations consider isolated Ag(I) and benzene species. This might be a reasonable approximation in C₆H₆·AgClO₄ where the Ag-O distance is 2.7 A, but not in this complex where the shortest Ag-Cl distance of 2.59 A is essentially a Ag-Cl single bond (2.51 A). Further, the local environment about the Ag(I) species is of sufficiently low symmetry that no simple hybrid metal orbital can be considered the acceptor as was the case in C₆H₆·Cu-AlCl₄.

The asymmetry in nearest metal-carbon distances of 2.92 and 2.47 A, both ± 0.06 A, is similar to that found in C_6H_6 ·CuAlCl₄ (2.15 and 2.30, both ± 0.03 A) and in C_6H_6 ·AgClO₄ (2.40 and 2.63, both ± 0.01 A), but is more pronounced. We believe that this asymmetry, although variable in magnitude, is a characteristic of M^+ ·C₆H₆ complexes. The wide variability may be due to packing considerations, but further structural investigation is necessary to establish this feature conclusively.

The present results, coupled with those from C_6H_6 · $CuAlCl_4$ and a recent refinement of C_6H_6 · $AgClO_4$, ²⁴ cast considerable doubt on nuclear magnetic resonance interpretations ²⁵ in which the benzene ring is allowed free rotation about its sixfold axis in C_6H_6 · $AgClO_4$.

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